MATHEMATICS STANDARD ARTICULATED BY GRADE LEVEL **Strand 1: Number and Operations** CONCEPT 2008 PO ITEM DESCRIPTION 2003 PO ITEM DESCRIPTION Compare and order real numbers including 1. Number Sense 1 Locate rational numbers on a number line. very large and small integers and decimals and fractions close to zero. 2 Classify real numbers as rational or 2 Identify irrational numbers. irrational. 3 Classify real numbers as rational or irrational. Solve problems that involve absolute 3 value.* 1 1 Select the grade-level appropriate operation to 2. Numerical Solve contextual problems including word solve word problems. problems with factors, multiples, divisibility **Operations** (with or without remainders), prime Solve word problems using grade-level 2 numbers, and composite numbers. appropriate operations and numbers. Describe the effect of multiplying and 2 dividing by numbers including the effect of multiplying and dividing a rational number by: zero. a number less than zero. a number between zero and one. one, or a number greater than one. * 3 Recognize the application of the properties 6 Apply grade-level appropriate properties to assist of the real number system: commutative. in computation. associative, distributive, identity, inverse, Use grade-level appropriate mathematical 8 and closure. terminology.

^{*} This performance objective is new to the 2008 Draft Mathematics Standard Articulated by Grade Level.

| | Strand 1: Number and Operations | | | | |
|---------------|---------------------------------|---|---------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 2. Numerical | 4 | Simplify numerical expressions using the | 3 | Determine the square of an integer. | |
| Operations | | order of operations that include grouping | 4 | Determine the square root of an integer. | |
| | | symbols, square roots, cube roots, absolute values, and positive exponents. | 5 | Identify squaring and finding square roots as inverse operations. | |
| | | | 7 | Apply the symbols "√" to represent square root, "±" to represent roots, and "{}" as grouping symbols. | |
| | | | 11 | Apply the symbols "√" to represent square root, "±" to represent roots, and "{}" as grouping symbols. | |
| | 5 | Use ratio and proportionality to solve problems involving percentages (including percent increase, percent decrease, and simple interest rates). | 9 | Calculate the missing value in a percentage problem. | |
| | 6 | Convert standard notation to scientific notation and vice versa (include positive and negative exponents). | 10 | Convert standard notation to scientific notation, and vice versa. | |
| | 7 | Simplify expressions using the rules of exponents. * | | | |
| 3. Estimation | 1 | Make estimates appropriate to a given situation by: | 1 | Solve grade-level appropriate problems using estimation. | |
| | | selecting the appropriate method of estimation, | 2 | Use estimation to verify the reasonableness of a calculation (e.g., Is 32 the square root of 64?). | |
| | | analyzing the effect of an estimation method on the | 3 | Express answers to the appropriate place or degree of precision (e.g., time, money). | |
| | | accuracy of results, and evaluating and justifying the reasonableness of results in a variety of situations that may or may not include calculator and computer results. | 4 | Verify the reasonableness of estimates made from calculator results within a contextual situation. | |

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| Strand 1: Number and Operations | | | | | |
|---------------------------------|---------|---------------------------------------|----------|---------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | A | 2003 PO | ITEM DESCRIPTION |
| 3. Estimation | 2 | Locate rational and common irrational | | S1C1-01 | Locate rational numbers on a number line. |
| | | numbers on a number line. | = | S1C1-02 | Identify irrational numbers. |
| | | | | S1C1-03 | Classify real numbers as rational or irrational. |

| | Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | | | |
|----------------------------------|---|--|---|---|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 1. Data Analysis (Statistics) | 1 | Solve problems by constructing, interpreting, and making calculations based on box and whisker plots, circle graphs, | 4 | Construct box-and-whisker plots. Interpret box-and-whisker plots, circle graphs, and scatter plots. | | |
| | and scatter plots (e.g., for scatter plots determine positive and negative correlation and line of best fit). | and scatter plots (e.g., for scatter plots determine positive and negative correlation | 9 | Solve contextual problems using scatter plots, box-and-whiskers plots, and double line graphs of continuous data. | | |
| | | 11 | Identify a line of best fit for a scatter plot. | | | |
| | 2 | Answer questions by selecting, creating, and interpreting contextual displays of data. | 3 | Determine the appropriate type of graphical display for a given data set. | | |
| | | | 5 | Answer questions based on box-and-whisker plots, circle graphs, and scatter plots. | | |
| | 3 | Describe how measures of center and the range relate to the shape of the distribution; informally identify outliers and determine their effect on mean, median, mode, interquartile range (midspread) and range. | 6 | Solve problems in contextual situations using the mean, median, mode, and range of a given data set. | | |

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| Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | | | |
|--|------------------|--|---------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 1. Data Analysis (Statistics) | 4 | Make inferences by comparing two or more data sets describing the same | 7 | Formulate reasonable predictions based on a given set of data. | |
| | | characteristic for two different populations or two subsets of the same population. | 8 | Compare trends in data related to the same investigation. | |
| | 5 | Determine whether information is represented effectively and appropriately | 3 | Determine the appropriate type of graphical display for a given data set. | |
| | | given a graph or a set of data by identifying sources of bias and compare and contrast the effectiveness of different representations of data. | 10 | Evaluate the effects of missing or incorrect data on the results of an investigation (e.g., Susie's teacher recorded a 39 instead of a 93 for her last quiz, what will happen to Susie's average?). | |
| | M05- S2C1-01 | Moved to Grade 5 | 1 | Formulate questions to collect data in contextual situations. | |
| | MCWR- S2C1-08 | Moved to College and Work Readiness | 12 | Distinguish between causation and correlation. | |
| 2. Probability | 1 | Determine the probability (theoretical or experimental) that a specific event will | 1 | Determine the probability that a specific event will occur in a 2-stage probability experiment. | |
| | | occur in a compound probability experiment. | 2 | Solve contextual situations using probability (e.g., If the probability of Michelle making a free throw is 0.25, what is the probability that she will make three free throws in a row?). | |
| | | | 3 | Predict the outcome of a grade-level appropriate probability experiment. | |
| | 2 | Interpret probabilities within a given context and compare the outcome of an | 4 | Record the data from performing a grade-level appropriate probability experiment. | |
| | | experiment to predictions made prior to performing the experiment. | 5 | Compare the outcome of an experiment to predictions made prior to performing the experiment. | |
| | | | 7 | Compare the results of two repetitions of the same grade-level appropriate probability experiment. | |
| | 3 | Use all possible outcomes (sample space) to determine the probability of dependent and independent events. | 6 | Distinguish between independent and dependent events. | |

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| | Strand 2: Data Analysis, Probability, and Discrete Mathematics | | | | | |
|--|--|---|---------|---|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 3. Discrete Mathematics – Systematic Listing and | 1 | Solve counting problems and represent counting principles algebraically including factorial notation. | 1 | Determine all possible outcomes involving the combination of two or more sets of objects (e.g., If you roll a six-sided number cube 4 times, how many possible outcomes are possible?). | | |
| Counting | | | 2 | Determine all possible arrangements given a set (e.g., How many ways can you arrange a set of 7 books on a shelf?). | | |
| | 2 | Represent, analyze, and solve counting problems that do or do not involve ordering and that do or do not involve repetitions. | 1 | Determine all possible outcomes involving the combination of two or more sets of objects (e.g., If you roll a six-sided number cube 4 times, how many possible outcomes are possible?). | | |
| | | Topoutions: | 2 | Determine all possible arrangements given a set (e.g., How many ways can you arrange a set of 7 books on a shelf?). | | |
| 4. Discrete Mathematics – Vertex-Edge Graphs | 1 | Use vertex-edge graphs and algorithmic thinking to represent and find solutions to practical problems related to Euler/Hamilton paths and circuits. | 1 | Solve contextual problems represented by vertexedge graphs. | | |
| • | 2 | Use directed graphs to solve problems; construct an adjacency matrix for a given directed graph. | 1 | Solve contextual problems represented by vertexedge graphs. | | |

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| | Strand 3: Patterns, Algebra, and Functions | | | | | |
|--------------------------------|--|---|---------|---|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 1. Patterns | 1 | Describe and extend numerical and geometric patterns using tables, graphs, | 1 | Communicate a grade-level appropriate iterative or recursive pattern, using symbols or numbers. | | |
| | | words, or symbols. | 2 | Extend a grade-level appropriate iterative or recursive pattern. | | |
| | | | 3 | Solve grade-level appropriate iterative or recursive pattern problems. | | |
| 2. Functions and Relationships | 1 | Write the rule of a simple function using formal algebraic notation. | 1 | Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model). | | |
| | 2 | Translate between different representations of linear expressions using symbols, graphs, tables, or written descriptions. | 3 | Determine whether a graph or table is related to a given equation of the form $y=ax^2$ where 'a' is a natural number. | | |
| | 3 | Use a table of values to graph an equation; describe the graph's characteristics. | S4C3-01 | Use a table of values to graph a linear equation. | | |
| | 4 | Describe a contextual situation that is depicted by a given graph; sketch a graph that models a given contextual situation. | 4 | Identify independent and dependent variables for a contextual situation. | | |
| | 5 | Determine if a relationship is a function given a graph. | * | | | |
| | 6 | Identify graphs as linear or nonlinear functions. | 2 | Distinguish between linear and nonlinear functions, given graphic examples. | | |

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| | Strand 3: Patterns, Algebra, and Functions | | | | | |
|-----------------|--|--|---------|---|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 3. Algebraic | 1 | Write or identify algebraic expressions, | 2 | Use variables in contextual situations. | | |
| Representations | | equations, or inequalities that represent a situation. | 3 | Translate a written sentence or phrase into an algebraic equation or expression, and vice versa (e.g., Three less than twice a number is 2 <i>n</i> -3.). | | |
| | | | 4 | Translate a sentence written in context into an algebraic equation involving two operations. | | |
| | | | 5 | Translate a contextual situation into an algebraic inequality (e.g., Joe earns more than \$5.00 an hour; therefore, <i>x</i> > 5). | | |
| | | | 6 | Identify an equation or inequality that represents a contextual situation. | | |
| | 2 | Evaluate algebraic expressions, including formulas, by substituting rational values for variables. | 1 | Evaluate algebraic expressions by substituting rational values for variables [e.g., $2(ab+ac+bc)$, when $a = 2$, $b = 3/5$, and $c = 4$]. | | |
| | 3 | Simplify algebraic expressions using order of operations and combining like terms (apply the identity, inverse, and associative properties). | 9 | Solve two-step equations with rational coefficients and integer solutions (e.g., $3x + 5 = 11$, $4x - 20 = 8$). | | |
| | 4 | Solve linear equations or inequalities. | 7 | Solve one-step equations with rational numbers as coefficients or as solutions. | | |
| | | | 8 | Solve one-step equations that model contextual situations. | | |
| | | | 9 | Solve two-step equations with rational coefficients and integer solutions (e.g., $3x + 5 = 11$, $4x - 20 = 8$). | | |
| | 5 | Analyze situations or solve problems using linear equations and inequalities. | 6 | Identify an equation or inequality that represents a contextual situation. | | |
| | 6 | Graph an inequality on a number line. | 10 | Identify an equation or inequality that represents a contextual situation. | | |
| | M08- S4C4-03 | Moved to Strand 4 Concept 4 | 11 | Solve a simple algebraic proportion. | | |
| | M08- S4C3-02 | Moved to Strand 4 Concept 3 | 12 | Solve applied problems using the Pythagorean theorem. | | |

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| Strand 3: Patterns, Algebra, and Functions | | | | | |
|--|---------|--|---------|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 4. Analysis of Change | 1 | Interpret relationships between symbolic linear expressions and graphs of lines by identifying and computing slope and intercepts. | 1 | Identify the slope of a line as the rate of change (the ratio of rise over run). | |
| | 2 | Solve contextual problems using simple rates. | 1 | Identify the slope of a line as the rate of change (the ratio of rise over run). | |
| | | | S5C1-01 | Describe how to use a proportion to solve a problem in context. | |

| Strand 4: Geometry and Measurement | | | | | |
|------------------------------------|---------|--|----------|---|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | |
| 1. Geometric Properties | 1 | Identify the properties of circles: radius, diameter, chords, tangents, secants, inscribed angles, control angles. | 7 | Recognize the relationship between inscribed angles and intercepted arcs. | |
| | | inscribed angles, central angles, intercepted arcs, circumference, and area. | 8 | Identify tangents and secants of a circle. | |
| | 2 | Predict results of combining, subdividing, and changing shapes of plane figures and solids (e.g., paper folding, tiling, and rearranging cut up pieces). * |) | | |

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| | Strand 4: Geometry and Measurement | | | | | |
|----------------------------|------------------------------------|---|---|---|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 1. Geometric Properties | 3 | Use proportional reasoning to justify relationships of congruence and similarity. | 1 | Draw a model that demonstrates basic geometric relationships such as parallelism, perpendicularity, similarity/proportionality, and congruence. | | |
| | | | 10 | Identify corresponding angles of similar polygons as congruent and sides as proportional. | | |
| | | | S4C4-06 | Solve problems using ratios and proportions, given the scale factor. | | |
| | | | S4C4-07 | Calculate the length of a side, given two similar triangles. | | |
| | | S5C1-01 | Describe how to use a proportion to solve a problem in context. | | | |
| | 4 | Determine the measure of angles created when parallel lines are cut by a transversal. | | Draw a model that demonstrates basic geometric relationships such as parallelism, perpendicularity, similarity/proportionality, and congruence. | | |
| | | | 6 | Identify the properties of angles created by a transversal intersecting two parallel lines (e.g., corresponding angles are congruent). | | |
| | 5 | Use the Pythagorean Theorem to solve problems. | S5C2-04 | Verify the Pythagorean theorem using an area dissection argument. | | |
| | M07- S4C1-02 | Moved to Grade 7 | 2 | Draw 3-dimensional figures by applying properties of each (e.g., parallelism, perpendicularity, congruency). | | |
| | M05- S4C4-06 | Moved to Grade 5 | 3 | Recognize the 3-dimensional figure represented by a net. | | |
| | M07- S4C4-06 | Moved to Grade 7 | 4 | Represent the surface area of rectangular prisms and cylinders as the area of their net. | | |
| | M05- S4C1-02 | Moved to Grade 5 | 5 | Draw regular polygons with appropriate labels. | | |
| | MHS- S4C1-07 | Moved to High School | 9 | Determine whether three given lengths can form a triangle. | | |

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| | STRAND 4: GEOMETRY AND MEASUREMENT | | | | | |
|-----------------------------|------------------------------------|---|---------|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | |
| 2. Transformation of Shapes | 1 | Identify lines of symmetry in plane figures or classify types of symmetries of plane figures. * | | Identify the planar geometric figure that is the result of a given rigid transformation. | | |
| | 2 | Model the result of rotations in multiples of 45 degrees of a figure about the origin. | 2 | Model a simple transformation on a coordinate grid (e.g., Translate right four units and down two units.). | | |
| | 3 | Describe the transformations that created a tessellation. | 1 | Identify the planar geometric figure that is the result of a given rigid transformation. | | |
| 3. Coordinate Geometry | 1 | Make and test a conjecture about how to find the midpoint between any two points on a coordinate plane. | 2 | Determine the midpoint given two points on a number line. | | |
| | 2 | Use the Pythagorean Theorem to find the distance between two points in a | 3 | Determine the distance between two points on a number line. | | |
| | | coordinate grid. | S3C3-12 | Solve applied problems using the Pythagorean theorem. | | |
| | M08- S3C2-03 | Moved to Strand 3 Concept 2 | 1 | Use a table of values to graph a linear equation. | | |
| 4. Measurement | 1 | Solve problems involving conversions within the same measurement system such as conversions involving square inches and square feet.* | | | | |
| | 2 | Calculate the area and perimeter of composite figures. | 1 | Solve problems for the area of a trapezoid. | | |
| | 3 | Solve geometric problems using ratios and proportions. | 6 | Solve problems using ratios and proportions, given the scale factor. | | |
| | | | S3C3-11 | Solve a simple algebraic proportion. | | |
| | 4 | Calculate the surface area and volume of rectangular prisms, cylinders, and | 2 | Solve problems involving the volume of rectangular prisms and cylinders. | | |
| | | composite solids. | 3 | Calculate the surface area of rectangular prisms or cylinders. | | |
| | | | 4 | Identify rectangular prisms and cylinders having the same volume. | | |

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| Strand 4: Geometry and Measurement | | | | |
|------------------------------------|-----------------|-----------------------------|---------|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION |
| 4. Measurement | | REMOVED | 5 | Find the measure of a missing interior angle in a triangle or quadrilateral. |
| | M08- S4C1-03 | Moved to Strand 4 Concept 1 | 7 | Calculate the length of a side, given two similar triangles. |

| Strand 5: Structure and Logic | | | | | | | |
|--|-----------------|--|---------|---|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | | |
| 1. Algorithms and Algorithmic Thinking | 1 | Create an algorithm to solve problems involving indirect measurements: | | | | | |
| | 2 | Describe when to use proportional reasoning to solve a problem. | 1 | Describe how to use a proportion to solve a problem in context. | | | |
| | | | S4C4-06 | Solve problems using ratios and proportions, given the scale factor. | | | |
| | M06- S5C1-01 | Moved to Grade 6 | 2 | Analyze algorithms. | | | |
| 2. Logic, Reasoning, Arguments, and Mathematical Proof | 1 | Develop the problem-solving strategy of writing an equation. | S3C2-01 | Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model). | | | |
| | | | S3C3-03 | Translate a written sentence or phrase into an algebraic equation or expression, and vice versa (e.g., Three less than twice a number is 2 <i>n</i> -3.). | | | |
| | | | S3C3-04 | Translate a sentence written in context into an algebraic equation involving two operations. | | | |
| | | | S3C3-06 | Identify an equation or inequality that represents a contextual situation. | | | |

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| Strand 5: Structure and Logic | | | | | | | |
|---|---------|--|--------------|---|--|--|--|
| CONCEPT | 2008 PO | ITEM DESCRIPTION | 2003 PO | ITEM DESCRIPTION | | | |
| 2. Logic, Reasoning, | 2 | Solve a non-routine problem by selecting and using a strategy. | S1C2-01 | Select the grade-level appropriate operation to solve word problems. | | | |
| Arguments, and Mathematical Proof | | | S1C2-02 | Solve word problems using grade-level appropriate operations and numbers. | | | |
| | 3 | Solve logic problems involving multiple variables, conditional statements, conjectures, and negation using words, charts, and pictures. | 1 | Solve a logic problem given the necessary information. | | | |
| | 4 | Make, validate, and justify conclusions and generalizations about linear relationships. | S3C2-01 | Describe the rule used in a simple grade-level appropriate function (e.g., T-chart, input/output model). | | | |
| | | | S3C2-03 | Determine whether a graph or table is related to a given equation of the form $y=ax^2$ where 'a' is a natural number. | | | |
| | | | S3C2-04 | Identify independent and dependent variables for a contextual situation. | | | |
| | 5 | Identify simple valid arguments using ifthen statements (e.g., All squares are rectangles. If quadrilateral ABCD is a rectangle, is it a square?). | 2 | Identify simple valid arguments using <i>ifthen</i> statements (e.g., All squares are rectangles. If quadrilateral ABCD is a rectangle, is it a square?). | | | |
| | 6 | Verify the Pythagorean Theorem using a valid argument. | 4 | Verify the Pythagorean theorem using an area dissection argument. | | | |
| | 7 | Model the relationship between the subsets of the real number systems. | 3 S1C1-03 | Model a contextual situation using a flow chart. Classify real numbers as rational or irrational. | | | |

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